

# Measuring the Stiffness of 2D Superconductors

Maya Klang<sup>1</sup> and Bessie Formigoni<sup>1</sup>  
Mentored by Nitsan Blau<sup>2</sup> and Prof. Amit Keren<sup>2</sup>

<sup>1</sup> The SciTech Program, Science and Technology Youth Center, Technion-Israel Institute of Technology, Haifa IL-32000, Israel  
<sup>2</sup> Department of Physics, Technion-Israel Institute of Technology, Haifa IL-32000, Israel



## Introduction & Motivation

- **Superconductivity** is a phenomenon of exactly zero electrical resistance and expulsion of magnetic fields (the Meissner effect) when superconductors are cooled down below  $T_C$ .
- **The Meissner effect** means that magnetic fields only penetrate the superconductor on a small scale, called the **penetration depth** ( $\lambda$ ).
- The **stiffness** of a superconductor is defined by  $\rho_s = \frac{1}{\mu_0 \lambda^2}$ .
- In superconductivity, the **London equation** describes the relation between the current density and the vector potential ( $A$ ):  
$$\mathbf{J} = -\rho_s \mathbf{A}$$
- In 2D material, the Meissner effect is very weak and the currents can only run on the surface. Thus, the London equation becomes,  
$$\mathbf{J}_s = -\frac{d}{\mu_0 \lambda^2} \mathbf{A} \delta(z)$$
where  $d$  is the thickness of the superconductor:
- Because magnetic fields can penetrate 2D superconductors, it is hard to measure their stiffness. We used a new method that doesn't apply magnetic field on the superconductor.
- Our goal is to measure the stiffness and the **critical temperature** of various thin superconducting **NbN (Niobium Nitride)** rings and studying the dependency of the above on the rings thickness.

## The Method

- We have been using an "infinitely" long coil in the center of a superconducting 2D ring. There is zero magnetic field outside, and finite vector potential which produces current density.

$$(B_{coil} = 0) \quad A_{coil} \propto \frac{I}{r} \hat{\theta} \longrightarrow J_{ring} \longrightarrow A_{ring}$$

- The flux of the ring through a pickup loop (radius  $R_{PL}$ ) is:

$$\Phi(z) = 2\pi R_{PL} \times A_{ring}(R_{PL}, z)$$

- $A$  is measured by moving the ring, which induces an electromotive force.
- The important relation is:

$$\frac{\Delta V_{ring}}{\Delta V_{coil}} = G \cdot A(R_{PL}, z=0)$$

Where  $A(R_{PL}, 0) \equiv \frac{A_{ring}(R_{PL}, 0)}{A_{coil}(R_{PL})}$ .

- $G \approx 2.7$  is a geometrical factor related to the gradiometer ( $G_{PL} = 1$ ).

- By measuring  $\Phi(z)$  (Fig. 1) we determine the solution of the normalized **Pearl equation** of our specific setup:

$$\nabla \times \nabla \times \mathbf{A} = -\frac{1}{\Lambda} \left( \mathbf{A} + \frac{1}{r} \hat{\theta} \right) \delta(z)$$

Where  $\Lambda = \frac{\lambda^2}{d}$  and  $A = \frac{A_{ring}(r, z)}{A_{coil}(R_{PL})}$

- We need to calculate  $A(R_{PL}, z=0)$  and fit the data, i.e. solve the Pearl equation.

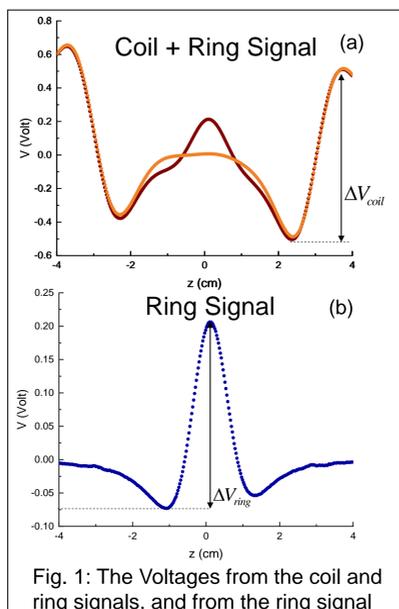


Fig. 1: The Voltages from the coil and ring signals, and from the ring signal

## The Experiment

- Our samples are rings of **NbN** (Fig. 2), which is a superconducting material. The **NbN** is placed on a silicon ring, covered by silicon oxide (Fig. 3).



$\varnothing_{in} = 1 [mm]$   
 $\varnothing_{out} = 4 [mm]$   
Fig. 2

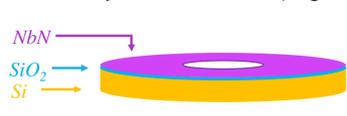
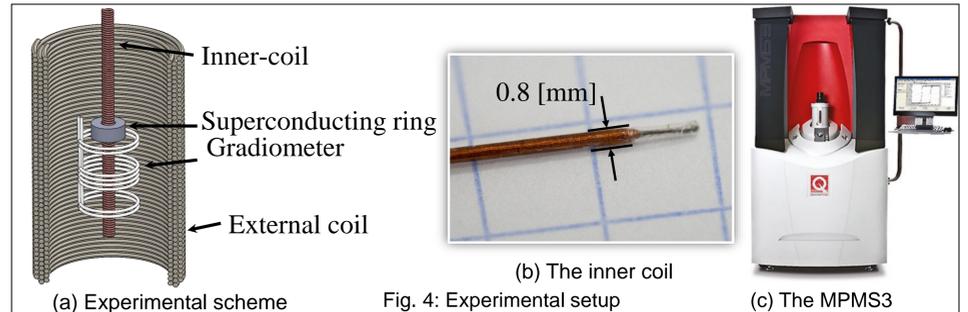


Fig. 3

- The measurements were made with ultra thin **NbN** rings: 3,5,10,15 [nm].

- When in bulk, the properties of **NbN** are:  $T_C \gg 16 [K]$ ,  $l \gg 200 [nm]$ .
- **Cu** coil: Length - 6 [cm]; Wire Thickness - 50 [μm]; Outer Diameter - 0.8 [mm]; 2400 turns (2 layers),  $R_{PL} = 8.5 [mm]$  (Fig. 4).



## Results

We use the solution to the Pearl Equation, along with the magnetic potential  $A$  as function of  $T[K]$  (Fig. 5), to calculate the **Pearl length**, from which we can extract the penetration depth (Fig. 6). The results showed a surprising difference for  $A$  between opposite current directions (Fig. 7).

$$\square \times \square \times \mathbf{A} = -\frac{1}{L} \mathbf{A} + \frac{1}{r} \hat{\theta} d(z) \longrightarrow \Lambda(A(R_{PL}, 0))$$

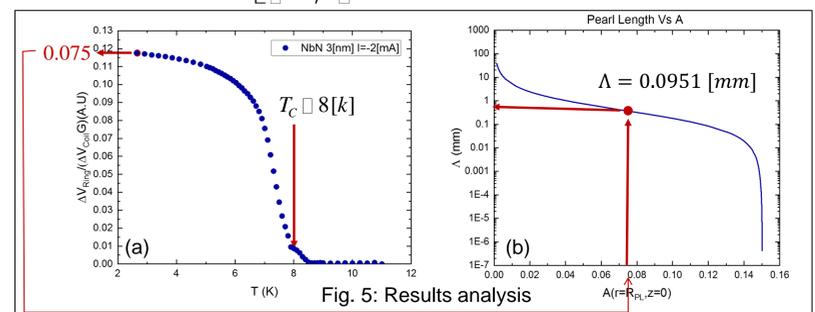


Fig. 5: Results analysis

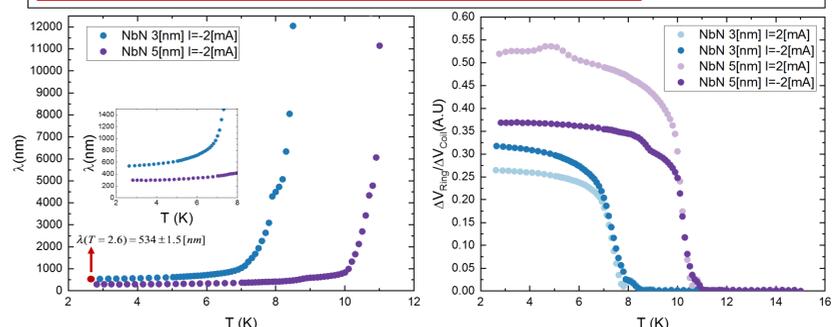


Fig. 6: The penetration depth

Fig. 7: Voltage ratio

## Concluding Remarks

- We used a new method of measuring the stiffness of 2D superconductor films, and compared the stiffness of a 3nm NbN ring, and a 5nm NbN ring.
- We found a surprising difference between the measurements of the same NbN ring when the current applied has an opposite sign. We assume the difference is because of a remnant magnetic field inside the measurement chamber.

## Acknowledgments

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## References

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